## ACTIVISM, STRATEGIC TRADING, AND MARKET LIQUIDITY

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### Share-holder Activism

- Activists play central role in modern corporate governance and are often successful in increasing the value of targeted companies (Icahn, Buffett, Ackman, Peltz, Loeb).
- Feb 2015 issue of The Economist called them "Capitalism's unlikely heroes."
  - Assets under management more than doubled since 2008 to close to \$120 billion of capital in 2014, where it attracted a fifth of all flows into hedge funds.
  - According to the Economist: "Last year Activists launched 344 campaigns against public companies, large and small. In the past five years one company in two in the S&P 500 index of Americas most valuable listed firms has had a big activist fund on its share register, and one in seven has been on the receiving end of an activist attack."

Share-holder Activism

### ACTIVISM: SCHEDULE 13D DISCLOSURE RULES

- Activists typically accumulate shares by trading anonymously in secondary markets.
- When their stake hits 5%, SEC requires they disclose within 10 days:
  - (I) their holdings and intentions (Brav et al. 2008)
     (e.g., Corporate governance action, Management shake-up, M&A transaction, Capital structure change, Cost reduction measures, Dividend payouts, Share buybacks, ...)
  - ${\rm (II)}\,$  all their trades during prior 60 days (CD and Fos (2015)):



- Schedule 13D activists:
  - own 7.2% stake on average on the filing date
  - increase share-holder value significantly (+6% excess returns in 30 days pre-filing) and persistently
  - target more liquid stocks (and trade when liquidity is high).

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- Big law firms such as Wachtell, Lipton, Rosen and Katz lobby the SEC to review the 13D disclosure rules to make it more difficult for activists to acquire shares *"in the interest of transparency and fairness for small shareholders."*

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- $\Rightarrow$  Raises questions about economic efficiency (and market liquidity).

### Background

- Link between market liquidity (price efficiency), corporate governance (activism), and firm value (economic efficiency):
  - Suppose activist can create (or destroy) value at some cost (e.g., governance).
  - Profitability depends on ability to buy (or sell) shares before market reflects full value (Maug (1998)).
  - Conversely, if market reflects value of activism, market liquidity may allow activist to sell out of her stake and hurt share-holders (Coffee (1991), Bhide (1993)).

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- Kyle (1985) proposes seminal model of strategic trading by informed investor:
  - Risk-neutral trader knows exogenous firm value V
  - Market marker sets price equal to expected value given she observes only total order flow (equal to informed trading plus noise).
  - $\Rightarrow$  (a) Optimal trading strategy, (b) Equilibrium price dynamics, (c) Market liquidity.

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  - $\Rightarrow$  (a) Optimal trading strategy, (b) Equilibrium price dynamics, (c) Market liquidity.
- We endogenize the liquidation value  $V(X_T)$  by modeling the effort choice of the activist as a function of the accumulated stake.

Background Model Setup Equilibrium Economic efficiency and market liquidity

### Types of activism

- Activist asks to increase payouts (larger effort leads to a larger change in firm value)
- Activist risk arbitrageur influences an M&A deal (larger effort leads to a higher probability of success)
- Activist requires to fire a CEO (binary outcome and non-binary effort)
- Activist nominates an alternative slate of board members (the outcome depends on activist's effort)

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It is an open question whether and how the relation between market liquidity and economic efficiency depends on the activism technology.

Background Model Setup Equilibrium Economic efficiency and market liquidity

### Related Literature

- The microstructure literature Kyle, 1985; Glosten and Milgrom, 1985; Easley and O'Hare, 1987; Back, 1992
- Take-over literature Grossman and Hart (1980), Shleifer and Vishny (1986), Kyle and Vila (1991)
- Corporate governance literature Coffee (1991), Bhide (1993), Admati, Pfleiderer, and Zechner (1994), Maug (1998)
- Dynamic model of governance DeMarzo and Urosevic (2006), Back, Li, Ljungqvist (2014), CD and Fos (2014)
- Market efficiency and disclosure rules: Grossman and Stiglitz (1980), Fishman and Haggerty (1995)
- Insider trading: Glosten (1989), Fishman and Haggerty (1992)

Background Model Setup Equilibrium Economic efficiency and market liquidity

# Model Setup

• Given a price function  $P(t, Y_t)$ , the activist seeks to maximize

$$\max_{v,\theta} \mathsf{E}\left[v X_T - C(v) - \int_0^T P(t, Y_t) \theta_t \, \mathrm{d}t \mid X_0\right].$$

where

- C(v) is arbitrary (convex) effort cost paid by activist to achieve v.
- $X_t = X_0 + \int_0^t \theta_s ds$  is aggregate stock position of activist.

(1)

Background Model Setup Equilibrium Economic efficiency and market liquidity

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- Market Maker has prior  $X_0 \sim N(\mu_X, \sigma_X^2)$  and observes total order flow  $Y_t$ :

$$dY_t = \theta_t dt + \sigma dZ_t$$

where  $Z_t$  is standard Brownian motion.

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• An equilibrium is a pair  $(P, \theta)$  s.t. trading strategy  $\theta$  maximizes (1) given P and

$$P(t, Y_t) = \mathsf{E}\left[V(X_T) \mid \mathcal{F}_t^Y\right]$$
(2)

for each t, given  $\theta$  and where  $V(x) = \operatorname{argmax}_{v} \{ vx - C(v) \}$ 

Background **Model Setup** Equilibrium Economic efficiency and market liquidity

## Some Examples of Cost function

• Symmetric quadratic (continuous) cost:  $C(v) = (v - v_0)^2/(2\psi)$ :

Linear  $V(x) = v_0 + \psi x$ 

Background Model Setup Equilibrium Economic efficiency and market liquidity

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$$C(v) = \begin{cases} (v - v_0)^2/(2\psi) & \text{if } v \ge v_0 \,, \\ \infty & \text{otherwise} \,. \end{cases}$$

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• Exponential case  $C(v) = \frac{1}{\psi} v \ln(\frac{v}{v_0}) - \frac{1}{\psi} v$ 

Strictly convex  $V(x) = v_0 e^{\psi x}$ 

Background Model Setup Equilibrium Economic efficiency and market liquidity

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• Binary (all or nothing): It costs c > 0 to increase stock value from  $v_0$  to  $v_0 + \Delta$ .

Digital 
$$V(x) = v_0 + \Delta \mathbf{1}_{[c/\Delta,\infty)}(x)$$

### Equilibrium

#### Theorem

The pricing rule  $P(t, Y_t) = E[h(Y_T) | \mathcal{F}_t^Y]$  with  $h(y) = V(\mu_x + \Lambda y)$ and the trading strategy:

$$\theta_t = \frac{1}{T - t} \frac{(X_t - \mu_x - \Lambda Y_t)}{\Lambda - 2}, \qquad (3)$$

where  $\Lambda = 1 + \sqrt{1 + \frac{\sigma_x^2}{\sigma^2 T}}$  only depends on the signal to noise ratio, constitute an equilibrium such that:

- $dP(t, Y_t) = \lambda(t, Y_t) dY_t$  with  $\lambda(t, y) = \frac{\partial P(t, y)}{\partial y}$ .
- Price impact  $\lambda(t, Y_t)$  is a martingale.
- $P(T, Y_T) = V(X_T)$  almost surely.
- $\mathsf{E}[\theta_t \mid \mathcal{F}_t^Y] = 0.$

• 
$$X_T \sim \text{Normal}\left[\mu_x, (\sigma\sqrt{T} + \sqrt{\sigma^2 T + \sigma_x^2})^2\right].$$

Background Model Setup Equilibrium Economic efficiency and market liquidity

### Equilibrium trading strategy

- $dY_t = \theta_t dt + \sigma dZ_t$  is a Brownian Motion with volatility  $\sigma$  on its own (i.e., market maker's) filtration
  - This implies that the optimal trading strategy is inconspicuous.

Background Model Setup Equilibrium Economic efficiency and market liquidity

### EQUILIBRIUM TRADING STRATEGY

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  - This implies that the optimal trading strategy is inconspicuous.
- Remarkably, the optimal trading strategy,  $\theta_t = \frac{1}{T-t} \frac{(X_t \mu_x \Lambda Y_t)}{\Lambda 2}$ , is independent of the effort cost (C(v), V(x)) when expressed as a function of  $Y_t, X_t$ .
  - Instead, the cost function C(v) determines V(x) and thus affects the price function P(t, Y) and the amount of effort expended.

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  - Instead, the cost function C(v) determines V(x) and thus affects the price function P(t, Y) and the amount of effort expended.
- Different from Kyle, the optimal trading strategy depends positively on the number of accumulated shares  $(X_t)$ 
  - $\rightarrow$  Amplification effect: The informed (activist) more than offsets the cumulative noise trading demand because the value of activism increases with activist's ownership.
  - $\rightarrow$  Evidence on activists' trading strategies
  - ightarrow The endogenous value of the firm depends on the amount of realized liquidity trading.

#### Examples: the symmetric quadratic model

#### EXAMPLE

In the symmetric quadratic model,  $V(x) = v_0 + \psi x$ , so

$$h(y) = v_0 + \psi \mu_x + \psi \Lambda y \,.$$

The price function at any time  $t \leq T$  is given by:

$$P(y,t) = v_0 + \psi \mu_x + \psi \Lambda y \tag{4}$$

The price impact function is given by:

$$\lambda(\mathbf{y}, t) = \psi \Lambda \tag{5}$$

This case resembles the original Kyle model:

- Price impact is constant
- However,  $\lim_{\sigma\to 0} \lambda = \psi > 0$  ('endogenous uncertainty'!).

### EXAMPLES: THE ASYMMETRIC QUADRATIC MODEL

#### EXAMPLE

In the asymmetric quadratic model,  $V(x) = v_0 + \psi x^+$ , so

$$egin{aligned} \psi(y) &= v_0 + \psi \left( \mu_x + \Lambda y 
ight)^+ \ &= egin{cases} v_0 & ext{if } y < -rac{\mu_x}{\Lambda} \ v_0 + \psi \mu_x + \psi \Lambda \, y & ext{otherwise} \ . \end{aligned}$$

The price function at any time  $t \leq T$  is given by:

$$P(y,t) = v_0 + \psi(\mu_x + \Lambda y) \mathsf{N} \left[ \frac{\mu_x + \Lambda y}{\Lambda \sigma \sqrt{T - t}} \right] + \psi \Lambda \sigma \sqrt{T - t} \mathsf{n} \left[ \frac{\mu_x + \Lambda y}{\Lambda \sigma \sqrt{T - t}} \right]$$
(6)

The price impact function is given by:

$$\lambda(y,t) = \psi \Lambda N \left[ \frac{\mu_x + \Lambda y}{\Lambda \sigma \sqrt{T - t}} \right]$$
(7)

Model Setup Equilibrium Economic efficiency and market liquidity

## Symmetric VS. Asymmetric quadratic cost function



Model Setup **Equilibrium** Economic efficiency and market liquidity

# SYMMETRIC VS. ASYMMETRIC QUADRATIC COST FUNCTION



Background Model Setup **Equilibrium** Economic efficiency and market liquidity

## EXAMPLES: THE EXPONENTIAL MODEL

#### EXAMPLE

In the exponential model,  $V(x) = v_0 e^{\psi x}$ , so

$$h(y) = v_0 e^{\psi(\mu_x + \Lambda y)}$$

The price function at any time  $t \leq T$  is given by:

$$P(y,t) = v_0 e^{\psi \left(\mu_x + \Lambda y + \frac{1}{2}\Lambda^2 \sigma^2(T-t)\right)}$$
(8)

The price impact function is given by:

$$\lambda(y,t) = \Lambda P(y,t) \tag{9}$$

A Black-Scholes price process with a price-volume relationship.

Background Model Setup Equilibrium Economic efficiency and market liquidity

### Examples: the binary effort model

#### EXAMPLE

In the binary effort model,

$$V(x) = v_0 + \Delta \mathbf{1}_{[c/\Delta,\infty)}(x),$$

so

$$\begin{split} h(y) &= v_0 + \Delta \mathbf{1}_{[c/\Delta,\infty)} \left( \mu_x + \Lambda y \right) \\ &= \begin{cases} v_0 & \text{if } y < \frac{(c/\Delta - \mu_x)}{\Lambda} \,, \\ v_0 + \Delta & \text{otherwise} \,. \end{cases} \end{split}$$

It follows that the price function at any time  $t \leq T$  is given by:

$$P(y,t) = v_0 + \Delta N \left[ \frac{\mu_x + \Lambda y - c/\Delta}{\Lambda \sigma \sqrt{T - t}} \right]$$
(10)

The price impact is given by:  $\lambda(y, t) = \frac{\partial P(y, t)}{\partial y} = \Delta \frac{n \left[ \frac{\mu_X + \Lambda y - c/\Delta}{\Lambda \sigma \sqrt{T - t}} \right]}{\sigma \sqrt{T - t}}$ 

Motivation Model of Activism, Liquidity and Efficiency Conclusion Equilibrium Conclusion

#### Economic efficiency and market liquidity

• We measure economic efficiency by price (at time 0), which is the expected effort of the activist.

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Background Model Setup Equilibrium Economic efficiency and market liquidity

### ECONOMIC EFFICIENCY AND MARKET LIQUIDITY

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- We measure market liquidity by the expected average price impact  $(E[\frac{1}{T}\int_{0}^{T}\lambda_{s}ds] = \lambda_{0}).$
- Importantly, market liquidity  $(\lambda)$  can be affected by different channels:
  - Noise trading volatility ( $\sigma$ )  $\sim$  Trading tax or length of disclosure window.
  - Prior uncertainty about insider's position  $(\sigma_X) \sim$  Disclosure rules.
  - Initial block size  $(\mu_x)$ .
  - Productivity of the activist  $(\Delta, \psi) \sim$  Legal environment.

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  - Initial block size  $(\mu_x)$ .
  - Productivity of the activist  $(\Delta, \psi) \sim$  Legal environment.
- These channels also have different implications for economic efficiency.
  - ⇒ We consider separately the ex-ante impact at date 0 when  $Y_0 = 0$  of a change in  $\sigma, \mu_x, \sigma_x, \psi$  on price (economic efficiency) and price impact (market liquidity).

Background Model Setup Equilibrium Economic efficiency and market liquidity

## PRODUCTIVITY OF THE ACTIVIST

#### EXAMPLE

In all (symmetric, asymmetric quadratic, exponential, binary) models:

$$rac{\partial P}{\partial \psi} > 0 \quad ext{and} \quad rac{\partial \lambda}{\partial \psi} > 0$$

- Variation in activism productivity generates negative cross-sectional relation between economic efficiency and market liquidity, because uncertainty about the activist's position creates more adverse selection when she is more productive.
- The causality (activism  $\rightarrow$  liquidity) is reverse of what the literature has focused on.

Background Model Setup Equilibrium Economic efficiency and market liquidity

## PRIOR UNCERTAINTY ABOUT ACTIVIST'S POSITION

#### Example

In the symmetric quadratic model:  $\frac{\partial P}{\partial \sigma_x} = 0$  and  $\frac{\partial \lambda}{\partial \sigma_x} > 0$ 

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In the asymmetric quadratic model: 
$$\frac{\partial P}{\partial \sigma_x} > 0$$
 and  $\frac{\partial \lambda}{\partial \sigma_x} > 0$ 

A general result obtains (since  $\sigma_x$  is mean-preserving spread for  $X_T$ ):

#### Theorem

If V(x) is convex then  $\frac{\partial P}{\partial \sigma_x} \ge 0$  (and conversely if V(x) is concave)

If V(x) satisfies mild regularity conditions  $\frac{\partial \lambda}{\partial \sigma_x} > 0$ 

• If V(x) is convex then cross-sectional variation in  $\mu_x, \sigma_x$  creates a negative relation between economic efficiency and market liquidity, because activism  $\rightarrow$  liquidity.

Background Model Setup Equilibrium Economic efficiency and market liquidity

## PRIOR UNCERTAINTY ABOUT ACTIVIST'S POSITION - CONT.

#### Example

In the binary effort model, 
$$\frac{\partial P}{\partial \sigma_x} \geq 0 \iff \mu_x \leq c/\Delta$$
 and  $\frac{\partial \lambda}{\partial \sigma_x} > 0$ 

- Cross-sectional variation in  $\mu_x, \sigma_x$  creates a negative relation between economic efficiency and market liquidity if only if the expected initial take is too low to justify activism on its own.
- More uncertainty about the insider's position:
  - creates more adverse selection risk and makes markets less liquid.
  - increases the likelihood that actual stake  $X_0$  is large enough to become active if  $\mu_x \leq c/\Delta$ .

Background Model Setup Equilibrium Economic efficiency and market liquidity

### Noise trading volatility

#### EXAMPLE

In the symmetric quadratic model:  $\frac{\partial P}{\partial \sigma} = 0$  and  $\frac{\partial \lambda}{\partial \sigma} < 0$ 

#### Example

In the asymmetric quadratic model: 
$$\frac{\partial P}{\partial \sigma} > 0$$
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A general result obtains (since an increase in  $\sigma$  is mean-preserving spread for  $X_T$ ):

#### Theorem

If 
$$V(x)$$
 is convex then  $\frac{\partial P}{\partial \sigma} \ge 0$  (and conversely if  $V(x)$  is concave then  $\frac{\partial P}{\partial \sigma} \le 0$ )

However, comparative statics for market liquidity  $\lambda$  are less straightforward.

Background Model Setup Equilibrium Economic efficiency and market liquidity

## NOISE TRADING VOLATILITY - CONT.

#### EXAMPLE

In the binary effort model,

$$\left\{\frac{\partial P}{\partial \sigma} \geq 0 \iff \mu_x \leq c/\Delta\right\} \quad \text{and} \quad \left\{\frac{\partial \lambda}{\partial \sigma} < 0 \iff |\mu_x - c/\Delta|^2 < T\sigma^2\Lambda^2(\Lambda - 1)\right\}$$



# CONCLUSION

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  - Increase in noise trading does not necessary improve market liquidity.
  - The relation between activism and liquidity depends on the source of variation in either.
- The paper informs about consequences of policy change such as trading tax, changing disclosure rules, disclosure window, legal environment.