Discussion of Activism, Strategic Trading and Liquidity by K. Back, P. Collin-Dufresne, V. Fos and A. Ljungqvist

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The Model

- C(v) the cost of achieving price v
 - Remove overpaid managers then Δv , not v
 - True value then v is not a choice variable
 - Conduct trade that will bring the price to v
- Optimal holdings by the activist

$$G(x) = \max_{v} (vx - C(v))$$

$$V(x) = \arg \max_{v} (vx - C(v))$$

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It is not clear how to unwind the position.

Optimal holdings

Initially the activist has X_0 shares, while others know that this amount is distributed $N(\mu_x, \sigma_x)$. With time the number of shares changes as X_t .

Denote the cumulative number of shares purchased by time t by noise traders by Z_t , distributed N(0, σ).

Aggregated purchases are $Y_t = Z_t + X_t - X_0$.

Denote $P(t, Y_t)$ the share price at time t.

Not clear why the price P is path independent if we consider liquidity effects.

Activist choses to maximize

$$\mathsf{E}\left[G(X_T) - \int_0^T P(t, Y_t)\theta_t \,\mathrm{d}t \mid X_0\right]$$

Applying this dynamically the activist's value function at time t is

$$J(t, x, y) \stackrel{\text{def}}{=} \sup_{\theta} \mathsf{E} \left[G(X_T) - \int_t^T P(u, Y_u) \theta_u \, \mathrm{d}u \, \middle| \, X_t = x, Y_t = y \right]$$

Eventually this leads to the following equations:

$$-P+J_x+J_y=0\,,$$

 $J_t+rac{1}{2}\sigma^2 J_{yy}=0\,.$

Optimal trading strategy:

$$\theta_t = \frac{1}{T-t} \left(\frac{X_t - \mu_x - \Lambda Y_t}{\Lambda - 2} \right)$$

If you are close to T and still do not have the required amount, you will have to trade a lot, since (T-t) is close to zero!

A more realistic (and more difficult) task is to chose T dynamically.